

Calcium Activity in Astrocytes

Evan Cresswell

Intro

- View of Astrocytes has changed
- metabolic and structural support to modulating maintaining neural activity
- Wave of research has ebbed and flowed our perception
- These advances the product of enhanced imaging technique!

Goals

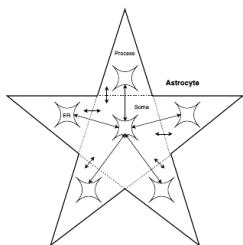
- What determines how local becomes global
- How can distinct astrocytic processes have independent activity
- What direction does information flow
- Do global and local affect the synapse differently
- What's up with the ER?

Model

- Like previous models, oscillations are initiated by interaction between the ER and the cytosol
- Both the ER and the cytosol have been compartmentalized
 - Used a Postnov model and modeled the soma and its branches individually
- Neurons – FitzHugh-Nagumo
- Synapse – sigmoid function
- Cytosol and ER – Keener and Sneyd calcium model with diffusion
- Secondary Messenger – sigmoid function triggered by synaptic

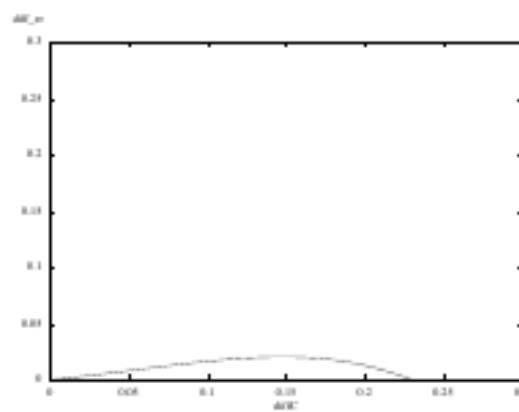
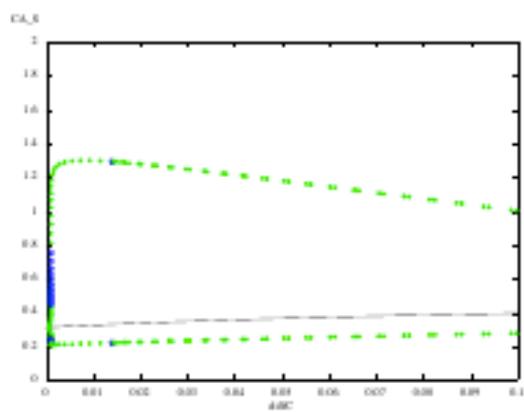
Activity

- Glial Messenger – sigmoid function triggered by calcium activity



| Section | Equations | Description |
|-----------------------------|--|----------------------------------|
| Pre – Synaptic Neuron | $\epsilon_1 \frac{dv_{pre_i}}{dt} = v_{pre_i} - \frac{v_{pre_i}^3}{3} - w_{pre_i}$ $\frac{w_{pre_i}}{dt} = v_{pre_i} + I_1 - I_{app}$ | <i>FitzHugh – Nagumo Mode</i> |
| Synapse | $\tau_s \frac{dz_i}{dt} = (1 + \tanh(s_s(v_{pre_i} - h_s)))(1 - z_i) - \frac{z_i}{d_s}$ | <i>activation variable</i> |
| Post – Synaptic Neuron | $\epsilon_2 \frac{dv_{post_i}}{dt} = v_{post_i} - \frac{v_{post_i}^3}{3} - w_{post_i}$ $\frac{w_{post_i}}{dt} = v_{post_i} + I_2 - I_{syn_i} - I_{glion_i}$ | <i>FitzHugh – Nagumo Mode</i> |
| Astrocytic Ca^{2+} | $\tau_c \frac{dC_{a_{pi}}}{dt} = r + \alpha w_{post_i} + \beta S_m - c_4 * f(Ca_{pi}, Ca_{er_i}) + d_c(Ca_s - Ca_{pi}) - Ca_{pi}$ $\epsilon_c \tau_c \frac{dC_{a_{er_i}}}{dt} = f(Ca_{pi}, Ca_{er_i}) + d_{er}(Ca_{er_2} - Ca_{er_1})$ $\tau_c \frac{dC_{a_s}}{dt} = -Ca_s - c_4 * f(Ca_s, Ca_e) + r + \sum_{i=1}^n d_c(Ca_{pi} - Ca_s)$ $\epsilon_c \tau_c \frac{dC_{a_{er_s}}}{dt} = f(Ca_s, Ca_{er_s}) + \sum_{i=1}^n d_{er}(Ca_{er_i} - Ca_{er_s})$ | <i>fast/slow Calcium Pathway</i> |
| Secondary Messenger | $\tau_{Sm} \frac{dS_{m_i}}{dt} = (1 + \tanh(s_{Sm}(z - h_{Sm}))(1 - S_{m_i}) - \frac{S_{m_i}}{d_{Sm}}$ | <i>activation variable</i> |
| Glutamate Messenger | $\tau_{Gm} \frac{dG_{m_i}}{dt} = (1 + \tanh(s_{Gm}(Ca_{pi} - h_{Gm}))(1 - G_{m_i}) - \frac{G_{m_i}}{d_{Gm}}$ | <i>activation variable</i> |

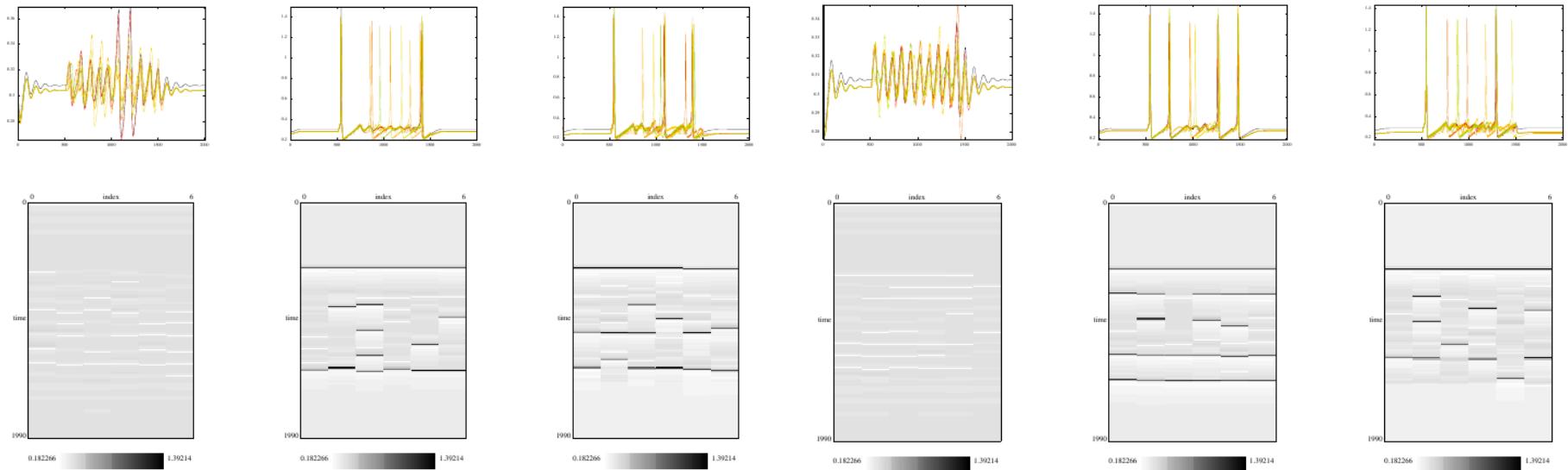
Periodic Behavior



Basic Calcium Dynamics

- First step to understand
- Able to reproduce similar dynamics to Postnov's paper
 - Changed alpha and beta

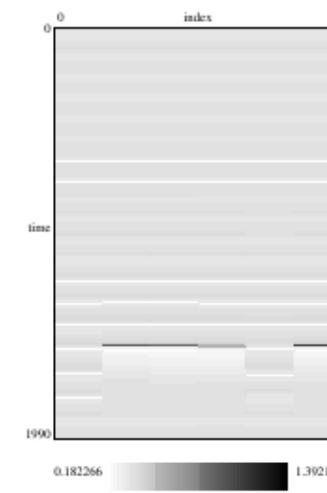
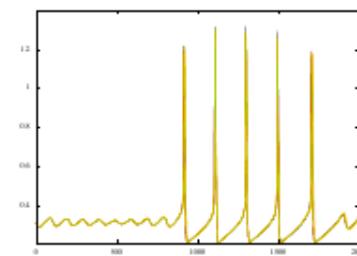
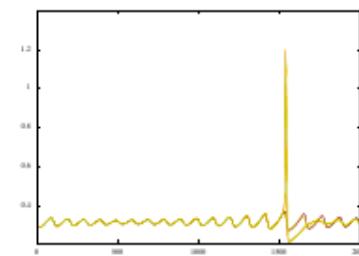
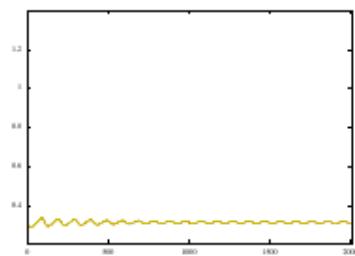
Basic Calcium Dynamics: alpha



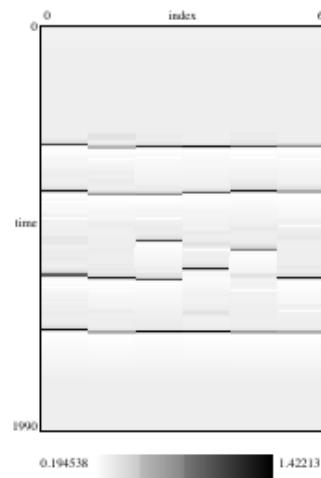
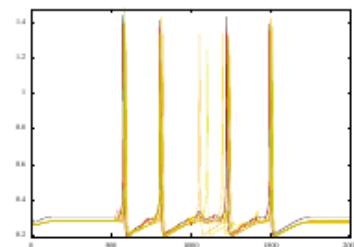
Alpha=.01, .05, .1

Higher firing
probability.

Basic Calcium Dynamics: beta



Basic Calcium Dynamics: Influence?

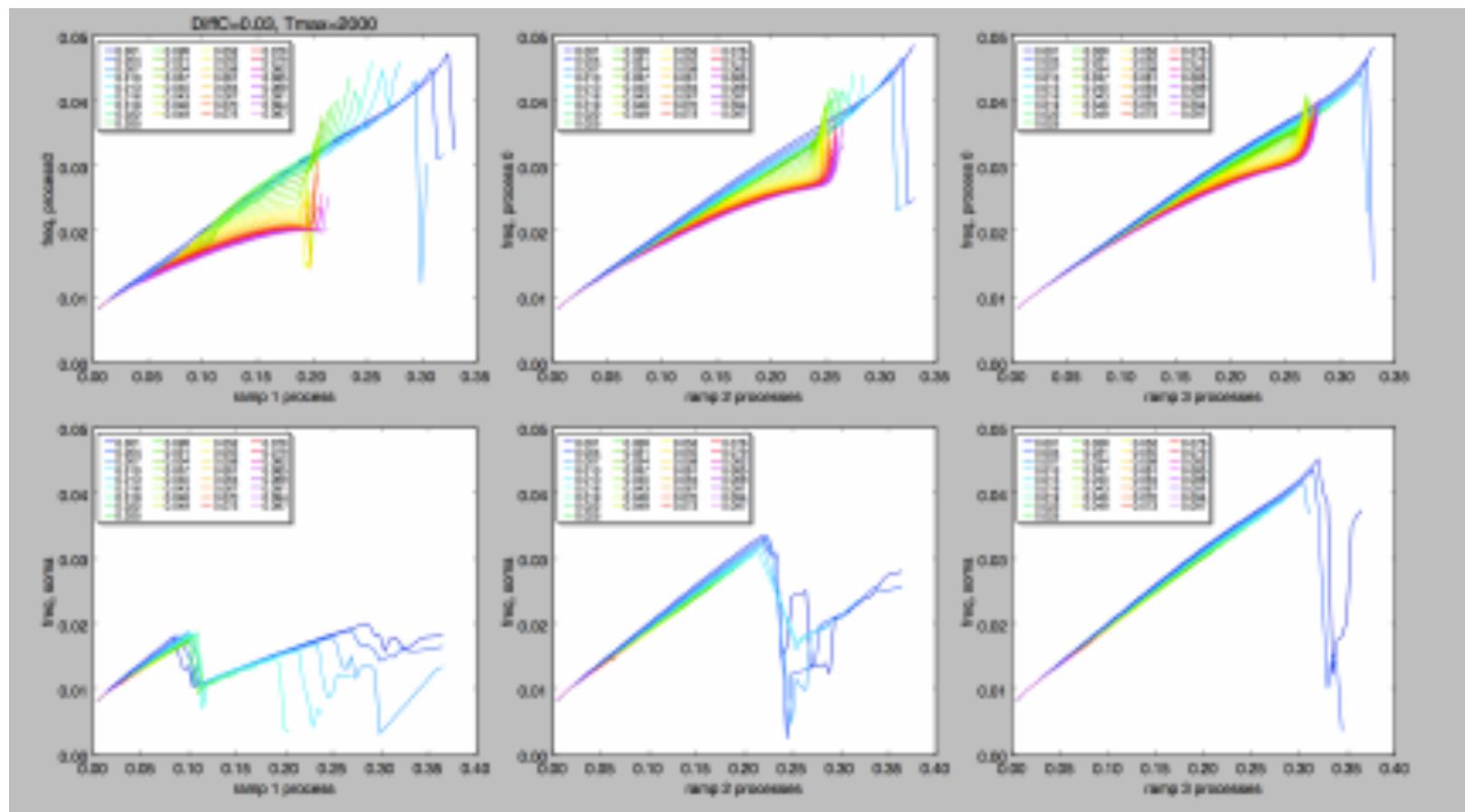


- Which direction is information going in?

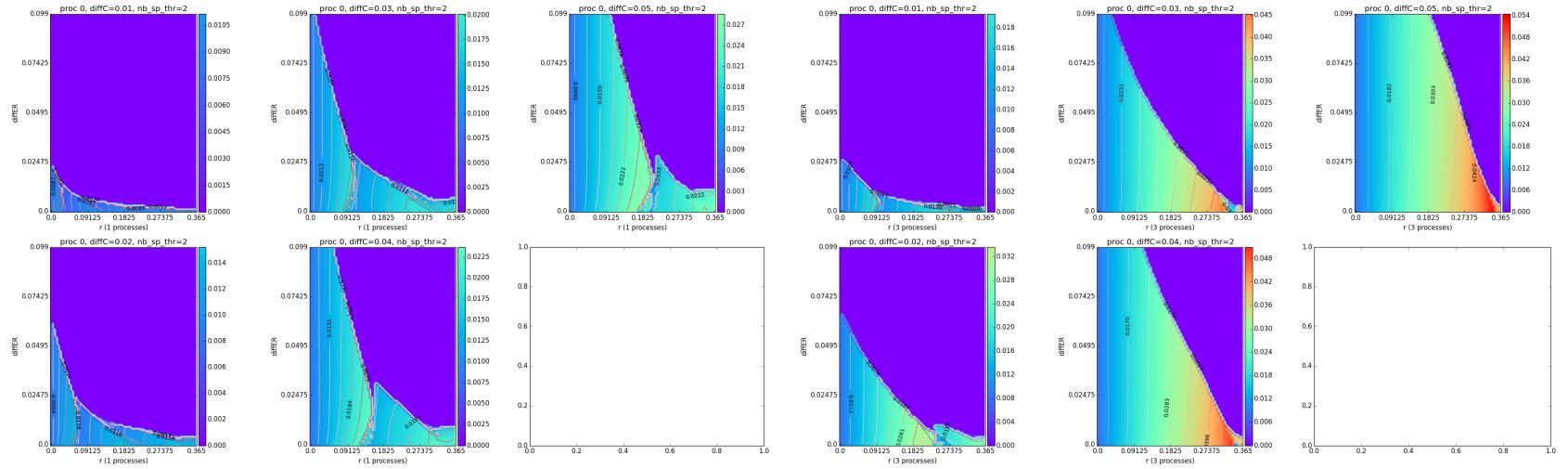
Batch Results

- Very exciting work!
 - Can tell us a lot of things about the behavior of our model
- Future directions?

Batch Results: Diffusion



Batch Results: Bifurcation



- Shows two par bifurcation diagram
- Great visualization
- Folds show emergence of harmonics!
 - What does this mean? artifact or jewel